

# Integer Programming Approach For Optimization Of Library Loan Policy

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**Abstract:** In the Library system, main objective is to provide the best services to the users. The purpose of this research is to develop a library system that house, implementing integrated procurement flow, return and borrowing books, so that the inter-library loan dealing can be done in an integrated manner, with the hope to facilitate members to borrow variety of books, thereby increasing library transactions. Interlibrary management system, library loan policy have been formed by using integer programming technique. This paper is prepared with a view to facilitate to users with loan period and maximum number of books can be borrowed.

**Index Terms:** Books, Integer programming, Landing-borrowing books, Maximum members facilitated

## 1 INTRODUCTION

LIBRARY management system is a difficult task. Library accounts are created for all currently enrolled students and employed faculty and staff after their registration. The purpose of this policy is to provide information about accessing and borrowing books from the Library. This policy applies to all staff and university students. University staff and students are registered to borrow books from the Library. For the purpose a card will be issued to the individuals by the library management. Staff and students of other institutions may also apply for registration and card may also be issued to them accordingly. The Library collects stores and uses borrower information for administrative purposes only. The information collected is confidential and will not be disclosed to third parties without the borrower's consent. A borrower is responsible for the safe keeping and return of all items or books borrowed from the Library and for the cost of repair or replacement of any item damaged or not returned. Restrictions are placed on the number of loans a user may have at any one time. Library staff and students are responsible for maintaining accurate contact details. The student/researcher email accounts are the main channel for communication concerning library borrowing. It is the responsibility of the management to control and monitor this account. All other borrowers need to notify the Library of any change of address (postal and email) at the earliest opportunity.

## 2 METHODOLOGY

### Integer Programming Model:

General integer programming model can be written as  
Optimize

$$Z = C_1X_1 + C_2X_2 + \dots + C_iX_j + \dots + C_nX_n$$

Subject to

$$a_{11}x_1 + a_{12}x_2 + \dots + a_{1j}x_j + \dots + a_{1n}x_n (\leq, =, \geq) b_1$$

$$a_{21}x_1 + a_{22}x_2 + \dots + a_{2j}x_j + \dots + a_{2n}x_n (\leq, =, \geq) b_2$$

$$\dots \dots \dots \dots \dots$$

$$a_{m1}x_1 + a_{m2}x_2 + \dots + a_{mj}x_j + \dots + a_{mn}x_n (\leq, =, \geq) b_m$$

$$x_j \geq 0, j = 1, \dots, n, x_j \text{ are all integers.}$$

The goal of every library is to facilitate maximum number of its members, but it is directly proportional to the number of resources they have, including many kinds of moderating factors like (time duration, number of books, memberships, members). This research include a general case of library for model development i.e A public library has two categories of books say  $x_1$  and  $x_2$ . Both can be borrowed by two kinds of memberships, Premium and Ultimate. A Premium member can be borrowed  $P_1$  books of category  $x_1$  and  $P_2$  books of category  $x_2$ . An Ultimate member can borrow  $U_1$  book of category  $x_1$  and  $U_2$  books of category  $x_2$ . Premium membership has limit of 'A' books and Ultimate has limit of 'B' books to be issued per month. A book of category  $x_1$  can be borrowed by  $M_1$  members while book of category  $x_2$  can be borrowed by  $M_2$  members in a month, as shown in the following table.

	Book $x_1$	Book $x_2$	Number of Books Availability
Premium Membership	$P_1$	$P_2$	A
Ultimate Membership	$U_1$	$U_2$	B
Number of Members to borrowed each Book	$M_1$	$M_2$	

Therefore IP model for general problem is

Maximize  $Z = M_1X_1 + M_2X_2$   
 Subject to  $P_1X_1 + P_2X_2 \leq A$   
 $U_1X_1 + U_2X_2 \leq B$   
 $X_1, X_2 \geq 0$  is an integer

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The above model is conducive to handle library management system in an effective manner and to the entire satisfaction of the users.

**Validity of Model:**

In order to check the validity of model, library of Asian Institute of Technology (AIT) Bangkok, Thailand visited for the purpose. Moreover the required data for the model has been collected and is as follows.

Number of books of Arts subjects:

$$A=104$$

Number of books of Science subjects:

$$B=76$$

Premium membership of library (includes science students only):  $P_1=2$

Premium membership of library(includes Arts students only):  $P_2=1$

Ultimate membership of library staff (includes science only)

$$U_1=1$$

Ultimate membership of library staff(includes Arts only):

$$U_2= 2$$

Number of members to borrow one book each of X1 category

$$M_1=6$$

Number of members to borrow one Book each of X2 category

$$M_2=11$$

Different categories of books borrowed by the members are indicated in the following table.

	Book X1	Book x2	Number of Books Availability
Premium Membership	2	1	104
Ultimate Membership	1	2	76
Number of Members to borrowed each Book	6	11	

Now the IP model for the above case is

$$\text{Maximize } Z = 6x_1 + 11x_2$$

$$\text{Subject to } 2x_1 + x_2 \leq 104$$

$$x_1 + 2x_2 \leq 76$$

$$x_1, x_2 \geq 0$$

Solution of the Problem

Step1. A basic feasible solution

Standard Form: Use slack variables  $S_1$  and  $S_2$  in the first and second constraint, we get

$$\text{Maximize } Z - 6x_1 - 11x_2 + 0.S_1 + 0.S_2 = 0$$

$$\text{Subject to } 2x_1 + x_2 + S_1 = 104$$

$$x_1 + 2x_2 + S_2 = 76$$

$$x_1, x_2, S_1, S_2 \geq 0$$

**Basic Solution:**

No. of variables:  $n = 4$ ; Basic variables:  $S_1$  and  $S_2$ .

No. of constraints:  $m = 2$ ; Non-basic variables:  $x_1$  and

$x_2$ .

By setting  $n - m = 4 - 2 = 2$  non-basic variables equal to zero.

So, put  $x_1 = 0, x_2 = 0$  in the constraints.

We get  $S_1 = 104, S_2 = 76$ . Both values are non-negative (positive). Thus a basic solution is a basic feasible solution.

**Step2. Optimality Test**

Write coefficients of all variables from standard form in the following table.

**Table 1**

Iteration	Basis	$x_1$	$x_2$	$S_1$	$S_2$	Solution	Ratio
1	Z	-6	-11	0	0	0	
(Starting)	$S_1$	2	1	1	0	104	104
	$S_2$	1	2	0	1	76	38

In z-equation there are still -ve numbers so solution is not optimal and go to step 3.

**Step 3. Entering variable**

The most -ve number is -11. So,  $x_2$  is an entering variable.

**Step 4. Leaving variable**

From ratio, 38 is the smallest number. So,  $S_2$  is a leaving variable.

**Step 5. Pivot equation**

Divide old pivot equation by 2, we get new pivot equation in the following table.

**Table 2**

Iteration	Basis	$x_1$	$x_2$	$S_1$	$S_2$	Solution	Ratio
2	Z						
	$x_2$ enters						
	$S_2$ leaves		$\frac{1}{2}$	0	$\frac{1}{2}$	38	

To complete the table we carry out the following type-2 computations.

1. New Z-equation

$$\begin{aligned} \text{Old Z-equation:} & \quad -6 \quad -11 \quad 0 \quad 0 \quad 0 \\ -(-11) \times \text{Pivot equation:} & \quad \frac{11}{2} \quad 11 \quad 0 \quad \frac{11}{2} \quad 418 \end{aligned}$$

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$$\text{New Z-equation} = \quad -\frac{1}{2} \quad 0 \quad 0 \quad \frac{11}{2} \quad 418$$

2. New  $S_1$  equation

$$\begin{aligned} \text{Old } S_1\text{-equation:} & \quad 2 \quad 1 \quad 1 \quad 0 \quad 104 \\ -(1) \times \text{Pivot equation:} & \quad -\frac{1}{2} \quad -1 \quad 0 \quad -\frac{1}{2} \quad -38 \end{aligned}$$


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New  $S_1$ - equation =  $\frac{3}{2}$  0 1  $-\frac{1}{2}$  66

The complete new table thus looks as follows:

**Table 3**

Iteration	Ba-sis	$x_1$	$x_2$	$S_1$	$S_2$	So-lu-tion	Ratio
2	Z	$-\frac{1}{2}$	0	0	$\frac{11}{2}$	418	
$x_1$ enters $S_1$ leaves	$S_1$	$\frac{3}{2}$	0	1	$-\frac{1}{2}$	66	44
	$x_2$	$\frac{1}{2}$	1	0	$\frac{1}{2}$	38	76

Step 2. There is still -ve number in Z-equation. So, go to step 3.

Step 3. Entering variable

The most -ve number is  $-\frac{1}{2}$ . So,  $x_1$  is an entering variable.

Step 4. Leaving variable

From ratio, 44 is the smallest number. So,  $S_1$  is a leaving variable

Step 5. Pivot equation

Divide old pivot equation by  $\frac{3}{2}$ , we get in the following table.

**Table 4**

Iteration	Basis	$x_1$	$x_2$	$S_1$	$S_2$	Solution
3	Z					
$x_1$ enters $S_1$ leaves	$x_1$	1	0	$\frac{2}{3}$	$-\frac{1}{3}$	44
	$x_2$					

To complete the table we carry out the following type-2 computations.

1. New Z-equation

Old Z-equation:  $-\frac{1}{2}$  0 0  $\frac{11}{2}$  418

$-\left(\frac{-1}{2}\right) \times$  Pivot equation:  $\frac{1}{2}$  0  $\frac{1}{3}$   $-\frac{1}{6}$  22

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New Z-equation = 0 0  $\frac{1}{3}$   $\frac{16}{3}$  440

2. New  $x_2$  equation

Old  $x_2$  e equation:  $\frac{1}{2}$  1 0  $\frac{1}{2}$  38

$-\left(\frac{1}{2}\right) \times$  Pivot equation:  $-\frac{1}{2}$  0  $-\frac{1}{3}$   $\frac{1}{6}$  -22

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New  $x_2$  equation = 0 1  $-\frac{1}{3}$   $\frac{2}{3}$  16

The complete new table thus looks as follows:

**Table 5**

Iteration	Basis	$x_1$	$x_2$	$S_1$	$S_2$	Solution
3 (Optimum)	Z	0	0	$\frac{1}{3}$	$\frac{16}{3}$	440
	$x_1$	1	0	$\frac{2}{3}$	$-\frac{1}{3}$	44
	$x_2$	0	1	$-\frac{1}{3}$	$\frac{2}{3}$	16

Step2. Optimality Test: There is no negative number in Z-equation. Stop the iterations and current solution is optimal.

Therefore, the optimal solution is

$x_1 = 44$

$x_2 = 16$  and

$Z_{max} = 440$

### 4 CONCLUSION

The library loan and borrow management system model for optimal user satisfaction has been developed. This model considers both the elements of the loan policy. That is loan period and maximum number of books a user may be borrowed. The user satisfaction is gauged by his satisfaction with these two fundamentals. The model also tender a more comprehensive and rational representation of the problem. More over the solution of the model may be easily acquired with the help of available soft ware.

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