Numerical Simulation Of A Highly Maneuvering Target In 2D Using The Bayesian Framework

Radhika MN, S S Parthasarathy, Mahendra Mallick

Abstract: In this paper we describe numerical simulation of a highly maneuvering target in 2D using the Bayesian framework. We consider accelerations of 3g, 4g, and 5g for the highly maneuvering target using the nearly constant turn (NCT) motion in the counter-clockwise and clockwise directions. The target has a sequence of nearly constant velocity (NCV) and NCT motions. We simulate true trajectories of the target in Monte Carlo runs using the prior distribution and the NCV and NCT dynamic models. A fixed moving target indicator (MTI) radar is used to generate range, azimuth, and radial velocity measurements.

Keywords: Bayesian framework, Highly maneuvering target, Monte Carlo simulation, Nearly constant turn (NCT), MTI radar measurement model

1. INTRODUCTION

Two commonly used frameworks in filtering are the Bayesian and Fisher frameworks [1], [6], [12], [28], [29], [31], [32]. The state of the target in the Bayesian framework is a random variable, whereas the state of the target in the Fisher framework is non-random. At present the Bayesian framework is regarded as the preferred model for filtering [1], [6], [28], [31], [32]. A filtering algorithm has a dynamic model and a measurement model. The dynamic model describes the motion of the target and the measurement model describes the relationship of the measurement on the target state and measurement noise. The famous Kalman filter (KF) algorithm [14] is based on the Bayesian framework. In the KF, the dynamic and measurement models are linear with additive zero-mean white Gaussian process and measurement noises [1], [6]-[8], [14], [28]. In addition, the initial state has a prior Gaussian distribution with known mean and covariance [1], [28], [31]. The initial state, the process noise, and measurement noise are assumed as independent [1], [6]-[7], [28], [31]. The KF is an optimal estimator in the minimum mean square error (MMSE) sense [1], [6]-[7], [28] under standard KF assumptions. However, many real-world problems are nonlinear in nature. The KF is not applicable to problems when the dynamic or/and measurement models are nonlinear [1], [6]-[8], [28]. An optimal filtering algorithm in the MMSE sense does not exist for a nonlinear filtering problem [1], [6]-[7], [28]. A number of approximate nonlinear filters have been proposed for nonlinear filtering problems. Commonly used nonlinear filtering algorithms are the extended Kalman filter (EKF) [1], [6]-[8], [20], [21], [28], [30], unscented KF (UKF) [13], [21], [28], cubature KF (CKF) [2], and particle filter (PF) [3-4], [28]. A maneuvering target is an accelerating target [19]. A non-maneuvering target moves with constant velocity (CV) or nearly CV (NCV) [6]-[7], [19]. For an accelerating target, the speed, direction of velocity, or both can change. Examples of a maneuvering target motion with one type of dynamic model are motions with nearly constant acceleration (NCA) and nearly constant turn (NCT) [4], [6]-[7], [19], [28]. In real-world scenarios, a target can move with multiple motions, such as a sequence of NCV, NCA, NCT, NCV, etc. [15], [21]. In such cases, a filtering algorithm using a single dynamic model is not applicable. A famous algorithm for a maneuvering target with multiple motion models is the interacting multiple model (IMM) estimator [6-8], [10-11], [21], [25], [28], which uses a fixed number of dynamic models for the full observation period.

When the number of dynamic models is high, improved filtering accuracy can be achieved by adaptively selecting a subset of the dynamic models as is done in the variable-structure IMM (VS-IMM) filter [17-19]. Typically, a highly maneuvering target can have an acceleration of greater than 2g [5], [9], [16], [27], where g is the acceleration due to gravity with a nominal value of 9.8 m/s². The acceleration of a target can be expressed in terms of the g-factor. Since the acceleration will depend on the type of target, it is important to consider the type of target while simulating trajectories of a target. Highly maneuvering targets can be ballistic missiles, cruise missiles, interceptors, or fighter aircraft. The speeds of a cruise missile and ballistic missile are around 1500 m/s and 5000 m/s, respectively. Bahari et al. [5] considered a target moving with constant acceleration, and the maximum acceleration had a value of about 3.2 g. In [9] Blackman et al. considered a highly maneuvering aircraft with a maximum acceleration of 3g moving with the NCT motion. Kumar et al. [16] studied interception of highly maneuvering targets using seeker-less interceptors. Accelerations of the interceptors in their study were 2g and 4g. Meng et al. [27] analyzed a low altitude (30 km) target moving in Earth’s atmosphere under the influence of Earth’s spherical gravitational field and atmospheric drag. The numerical value of the acceleration of the target is not available in this paper. Yang and Ji [33] studied a highly maneuvering aircraft with the NCA motion which had a maximum acceleration of about 3.7 g. In this paper we consider a fighter aircraft whose speed is around 370 m/s and which can have accelerations of 3g, 4g, or 5g. For simplicity we have assumed that the target moves in 2D (XY-plane) and consider a fixed MTI radar [20-22] in the XY-plane. In realistic scenarios, the target and radar can move in 3D in different planes as considered in [24]. In many published papers and books, the measurement function for azimuth is not correctly stated, and the domain of the azimuth measurement function is used as the real line \( \mathbb{R} \). Stated correctly, the domain and range of the azimuth measurement function are \( \mathbb{R}^2 \) and \( [0,2\pi) \), respectively. Our previous work in [23] has clearly explained this issue.

The main objectives of this paper are:
- Clearly describe simulation of true trajectories in Monte Carlo runs using the Bayesian framework.
- Emphasize the role of the prior distribution to generate distinct initial states in Monte Carlo runs.
• Simulate true trajectories for a highly maneuvering target using accelerations of 3g, 4g, and 5g.
• Explain variations of range, azimuth, and radial velocity with time as the target moves with NCV and NCT motions.
• Specifically, explain variation of azimuth in the interval \([0, 2\pi]\).

We use ":=" to define a quantity. An italic letter denotes a scalar quantity and a boldface lower or upper case Roman letter denotes a vector or a matrix. The transpose of a vector or matrix \(A\) is denoted as \(A^\top\). The organization of the paper is as follows. Sections 2 and 3 present the dynamic and measurement models. For circular motion in 2D, we present relationships among speed, angular velocity, and centripetal acceleration in Section 4. Section 5 presents numerical simulations and results, and Section 6 summarizes our contributions in the paper and discusses future work.

2. DYNAMIC MODELS

In this paper we consider the motion of a target in 2D. This section discusses in detail the discrete-time dynamical models used to represent different target motions for a highly maneuvering target. These motions are the NCV and NCT motions in clockwise and anti-clockwise directions. There are two types of discrete-time dynamic/kinematic models, discretized continuous-time model and direct discrete-time model [6]. We follow the discretized continuous-time model, since this naturally follows from Newton’s second law. The position and velocity components of the target state are denoted by \((x, y)\) and \((\dot{x}, \dot{y})\), respectively. The state vector of the target at time \(t_k\) for both the NCV and NCT model is defined by [4], [28]

\[
x_k := [x_k \ y_k \ \dot{x}_k \ \dot{y}_k].
\] (1)

We refer to the NCV, NCT in the anti-clockwise direction, and NCT in the clockwise direction as models 1, 2, and 3, respectively. The model index is used as a superscript in the state transition matrix, process noise, and process noise covariance matrix.

2.1. Nearly Constant Velocity Model

The dynamic model for the NCV motion is described by [1], [6-7], [20]

\[
x_k = F_{k-1} x_{k-1} + \omega_{k-1}^{(1)}
\] (2)

where \(F_{k-1}\) is the state transition matrix \(w_{k-1}^{(1)}\) is the integrated process noise (we shall use "process noise" for simplicity) in the time interval \((t_{k-1}, t_k)\) [6], [20]. We assume that the process noise is zero-mean, white, Gaussian with covariance \(Q_{k-1}^{(1)}\). The state transition matrix and process noise are described by [6], [20]

\[
F_{k-1}^{(1)} = \begin{bmatrix} 1 & 0 & T & 0 \\ 0 & 1 & 0 & T \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}
\] (3)

\[
E[w_{k-1}^{(1)}] = 0,
\] (4)

\[
E[w_{k-1}^{(1)}(w_{k-1}^{(1)})^\top] = \delta_{jk} Q_{k-1}^{(1)},
\] (5)

\[
Q_{k-1}^{(1)} = q_1 \begin{bmatrix} T^2/3 & 0 & T^2/2 & 0 \\ 0 & T^2/3 & 0 & 1/2 T^2 \\ T^2/2 & 0 & T & 0 \\ 0 & T^2/2 & 0 & T \end{bmatrix},
\] (6)

where \(\delta\) is the Kronecker delta, \(q_1\) is the power spectral density (PSD) of the X or Y components of the continuous-time acceleration process noise [6], [20].

2.2. Nearly Constant Turn Model

The dynamic models for the NCT motions are described by [4], [6], [28]

\[
x_k = F_{k-1}^{(j)} x_{k-1} + w_{k-1}^{(j)}, j = 2, 3,
\] (7)

where the state transition matrices are given by

\[
F_{k-1}^{(j)} = \begin{bmatrix} 1 & 0 & \sin(\omega_k^{(j)} T) & -1 - \cos(\omega_k^{(j)} T) \\ 0 & 1 & -\cos(\omega_k^{(j)} T) & \sin(\omega_k^{(j)} T) \\ 0 & 0 & \cos(\omega_k^{(j)} T) & -\sin(\omega_k^{(j)} T) \\ 0 & 0 & \sin(\omega_k^{(j)} T) & \cos(\omega_k^{(j)} T) \end{bmatrix}, j = 2, 3
\] (8)

\[
\omega_{k-1}^{(j)} = \kappa^{(j)} \frac{\alpha_m}{\sqrt{x_k^{2} + y_k^{2}}}, j = 2, 3
\] (9)

where \(\alpha_m > 0\) is typical maneuver acceleration and \(\kappa^{(2)}\) and \(\kappa^{(3)}\) are 1 and -1 corresponding to counter-clockwise and clockwise NCT motions, respectively. The process noise covariance matrices are

\[
Q_{k-1}^{(j)} = q_j \begin{bmatrix} T^2/3 & 0 & T^2/2 & 0 \\ 0 & T^3/3 & 0 & 1/2 T^2 \\ T^2/2 & 0 & T & 0 \\ 0 & T^2/2 & 0 & T \end{bmatrix}, j = 2, 3
\] (10)

where \(q_2\) and \(q_3\) are the PSD of the process noise for models 2 and 3, respectively [4], [6], [28]. We use \(q_2 = q_3\).

3. MEASUREMENT MODEL

A moving target indicator (MTI) radar measures the range, bearing (or azimuth), and radial velocity of the target [20-22], [24]. We assume that the radar is at a fixed position \(s = [x_s \ y_s]\). Let \(p_k\) and \(v_k\) denote the position and velocity of the target at time \(t_k\),

\[
p_k = [x_k \ y_k],
\] (11)

\[
v_k = [\dot{x}_k \ \dot{y}_k].
\] (12)

The range vector at time \(t_k\) is given by

\[
\tau_k = p_k - s.
\] (13)

The range of the target from the sensor at time \(t_k\) is the magnitude of the range vector

\[
r_k = \| p_k - s \| = \sqrt{(x_k - x_s)^2 + (y_k - y_s)^2}.
\] (14)
where \( \| \mathbf{p}_k - \mathbf{s} \| \) represents the \( L_2 \) norm of the range vector. The unit vector \( \mathbf{u}_k \) along the radar line-of-sight (LOS) or the range vector is defined by

\[
\mathbf{u}_k := \frac{\mathbf{r}_k}{\| \mathbf{r}_k \|} = \frac{(\mathbf{p}_k - \mathbf{s})}{\| \mathbf{p}_k - \mathbf{s} \|}.
\]

(15)

The radial velocity of the target is defined as the projection of the target velocity along the RLOS as shown in Fig. 1 and is given by [20-22], [24]

\[
v_{r,k} := \mathbf{n}_k \cdot \mathbf{u}_k = \frac{1}{r} \left[ (x_k - x_s)x_k + (y_k - y_s)y_k \right].
\]

(16)

Let \( \alpha_k \) be the angle between the velocity of the target and the RLOS at time \( t_k \) (see Fig. 1). Then the radial velocity at time \( t_k \) can also be written as

\[
v_{r,k} = v_k \cos \alpha_k,
\]

(17)

where \( v_k \) is the speed of the target at time \( t_k \). Fig. 1 defines the true range, azimuth, and radial velocity of the target at time \( t_k \).

Figure 1. Definition of true range, azimuth, and radial velocity.

From Fig. 1 and (17), we find that when the target velocity is along or opposite to the RLOS, the radial velocity has the maximum and minimum values of \( v_k - \omega r \) and \( v_k + \omega r \), respectively. The radial velocity is zero when the target velocity is perpendicular to the RLOS. Let \( \mathbf{z}_k \) denote the measurement of the MTI radar at time \( t_k \). The measurement model for the MTI radar is described by [20-22], [24]

\[
\mathbf{z}_k = \mathbf{h}(x_k) + \mathbf{n}_k,
\]

(18)

where

\[
\mathbf{z}_k := [z_{k,r} \ z_{k,\theta} \ z_{k,\varphi}],
\]

(19)

\[
\mathbf{n}_k := [n_{k,r} \ n_{k,\theta} \ n_{k,\varphi}],
\]

(20)

\[
\mathbf{h}(x_k) = \begin{bmatrix} \frac{1}{r_k} \cdot \frac{\sqrt{(x_k - x_s)^2 + (y_k - y_s)^2}}{\tan^{-1}(x_k - x_s, y_k - y_s)} \\ \frac{1}{r_k} \cdot \frac{(x_k - x_s)y_k + (x_k - y_s)x_k}{(x_k - x_s)^2 + (y_k - y_s)^2} \\
\end{bmatrix},
\]

(21)

\[
r_k > 0, \beta_k \in [0, \pi),
\]

(22)

where \( h \) is the nonlinear measurement function and \( \mathbf{n}_k \) is a zero-mean white Gaussian measurement noise with covariance \( \mathbf{R} \),

\[
E[\mathbf{n}_k] = \mathbf{0},
\]

(23)

\[
\mathbf{n}_k \sim \mathcal{N}(\mathbf{n}_k; 0, \mathbf{R}),
\]

(24)

\[
\mathbf{R} = \text{diag}(\sigma_{r_0}^2, \sigma_{\theta_0}^2, \sigma_{\varphi_0}^2),
\]

(25)

where \( \sigma_{r_0}, \sigma_{\theta_0}, \sigma_{\varphi_0} \) are the standard deviations (SDs) of range, azimuth, and radial velocity, measurement errors, respectively.

3.1. Remark on Azimuth Measurement Function

We note that in (21), \( x_k - x_s \) and \( y_k - y_s \) lie in \( \mathbb{R} \). Therefore, the domain and range of the azimuth measurement function \( h_\theta = \beta \) are \( \mathbb{R} \) and \([0, 2\pi)\), respectively, as explained in [23]. For the azimuth measurement function, many published papers and books use

\[
h_\theta = \beta = \tan^{-1}(x_k - x_s, y_k - y_s).
\]

(26)

In (26), the domain and the range of the azimuth measurement function \( h_\theta \) are \( \mathbb{R} \) and \((-\pi/2, \pi/2)\), respectively, and hence do not represent correct results. In sub-section 5.5.2, we clearly describe the variation of the azimuth measurement function for the 4g acceleration scenario in the range \([0, 2\pi)\).

4. RELATIONS AMONG SPEED, ANGULAR VELOCITY, AND ACCELERATION

Consider a target moving in a plane in a circular arc of radius \( R \) with constant speed \( v \) and constant angular velocity \( \omega \). Let \( \alpha \) be the centripetal acceleration of the target. Then we have

\[
v = \alpha R
\]

(27)

\[
\alpha = \frac{v^2}{R} = \frac{v R}{v} = v \omega.
\]

(28)

Suppose the direction of velocity changes by an amount \( \Delta \theta \) during time interval \( \Delta t \). Since the angular velocity is constant,

\[
\omega = \Delta \theta / \Delta t.
\]

(29)

Therefore, from (28) and (29) we get

\[
v = \alpha / \omega = a \Delta t / \Delta \theta.
\]

(30)

Suppose in 60 seconds, \( \Delta \theta = 2\pi \text{rad} \) and \( a = 4g \). Using (29), the speed is about 374.332 m/s. We have used this value for the constant speed in all three scenarios where the target accelerations are \( 3g, 4g, \) and \( 5g \). The values of acceleration, speed, angular velocity, and radius of the arc are shown in Table 1 for these three scenarios.

Table 1. Variation of angular velocity and radius with acceleration.

<table>
<thead>
<tr>
<th>Acceleration</th>
<th>Speed (m/s)</th>
<th>( \omega ) (deg/s)</th>
<th>( R ) (m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>3g</td>
<td>374.332</td>
<td>4.5</td>
<td>4766.138</td>
</tr>
<tr>
<td>4g</td>
<td>374.332</td>
<td>6.0</td>
<td>3574.603</td>
</tr>
<tr>
<td>5g</td>
<td>374.332</td>
<td>7.5</td>
<td>2859.683</td>
</tr>
</tbody>
</table>
5. NUMERICAL SIMULATION AND RESULTS

We consider a highly maneuvering target moving in 2D. The target can have an acceleration of 3g, 4g, or 5g during the NCT motion as shown in Figs. 2, 3, or 4, respectively.

5.1. Target Parameters

The prior mean and variance of the target and PSD of the process noise for the NCV and NCT motions are shown in Table 2.

Table 2. Parameters of target.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Prior mean position</td>
<td>(1000, 20000) m</td>
</tr>
<tr>
<td>Prior mean velocity</td>
<td>(374.332,0) m/s</td>
</tr>
<tr>
<td>Variance of prior position</td>
<td>(40^2, 40^2) m^2</td>
</tr>
<tr>
<td>Variance of prior velocity</td>
<td>(4^2, 4^2) (m/s)^2</td>
</tr>
<tr>
<td>NCV: PSD of process noise</td>
<td>0.1 m^2/s^3</td>
</tr>
<tr>
<td>NCT: PSD of process noise</td>
<td>0.01 m^2/s^3</td>
</tr>
</tbody>
</table>

From Table 1, let \( \omega_1, \omega_2, \) and \( \omega_3 \) represent angular velocities of 4.5, 6.0, and 7.5 deg/s for the 3g, 4g, or 5g acceleration scenarios, respectively. Motion types in various segments shown in Figs. 2, 3, and 4 are summarized in Table 3.

Table 3. Type of motion in different segments.

<table>
<thead>
<tr>
<th>Segment</th>
<th>Time Duration (s)</th>
<th>Type of Motion</th>
<th>( \omega )</th>
</tr>
</thead>
<tbody>
<tr>
<td>AB</td>
<td>60</td>
<td>NCV</td>
<td>0</td>
</tr>
<tr>
<td>BC</td>
<td>30</td>
<td>NCT</td>
<td>( \omega_1, \omega_2, \text{ or } \omega_3 )</td>
</tr>
<tr>
<td>CD</td>
<td>60</td>
<td>NCV</td>
<td>0</td>
</tr>
<tr>
<td>DE</td>
<td>30</td>
<td>NCT</td>
<td>( -\omega_1, -\omega_2, \text{ or } -\omega_3 )</td>
</tr>
<tr>
<td>EF</td>
<td>60</td>
<td>NCV</td>
<td>0</td>
</tr>
</tbody>
</table>

5.2. Prior Distribution

Figs. 5 and 6 show the initial position and velocity components, respectively, from 500 Monte Carlo runs using the prior distribution.

Figure 2. True target trajectory from the first Mont Carlo run with 3g and -3g accelerations and MTI sensor position.

Figure 3. True target trajectory from the first Mont Carlo run with 4g and -4g accelerations and MTI sensor position. The LOS is tangent to the circular arc at G and H. Thus, the radial velocity has local maxima at G and H.

Figure 4. True target trajectory from the first Mont Carlo run with 5g and -5g accelerations and MTI sensor position.

Figure 5. Initial X and Y coordinates from 500 Monte Carlo runs using the prior distribution of position.

Figure 6. Initial X and Y components of velocity from 500 Monte Carlo runs using the prior distribution of velocity.
5.3. MTI Radar Parameters
Table 4 presents MTI sensor position and measurement parameters.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>MTI radar position</td>
<td>(12500, 0) m</td>
</tr>
<tr>
<td>Range SD</td>
<td>10 m</td>
</tr>
<tr>
<td>Azimuth SD</td>
<td>0.001 rad</td>
</tr>
<tr>
<td>Radial velocity SD</td>
<td>1 m/s</td>
</tr>
<tr>
<td>Measurement time interval</td>
<td>0.5 s</td>
</tr>
<tr>
<td>Number of measurements</td>
<td>481</td>
</tr>
</tbody>
</table>

5.4. True Trajectories
Target true trajectories from 500 Monte Carlo runs for 3g, 4g, and 5g accelerations are presented in Figs. 7, 8, and 9, respectively. We observe from Figs. 7-9 that there is a small spread of positions at the initial time due to the prior distribution. The spread among the trajectories gradually increases with time due to process noise and nonlinear dynamic models.

We present Fig. 11 with the beginning and end points of various segments to explain the variation of range with the measurement index in the first Monte Carlo run. As the target moves from A to B in Fig. 3 with the NCV motion, the range decreases and reaches its minimum when the target is right above the MTI sensor. Then the range gradually increases as the target moves towards D and reaches a local maximum at a point before the end point of the arc BC. Next, the range decreases as the target moves towards D and at the midpoint of CD, it has a local minimum. Similar variations in range are explained as the target moves from midpoint of CD to D, then to E, midpoint of EF, and F. Three local minima of range in Fig. 11 correspond to midpoints of segments AB, CD, and EF. Two local maxima of range in Fig. 9 appear before the end points of arcs BC and DE.

5.5. MTI Sensor Measurements
We have chosen the scenario for the 4g acceleration to present plots for the range, azimuth, and radial velocity measurements.

5.5.1. Range Measurements
Fig. 10 presents range measurements corresponding to 500 Monte Carlo runs in Fig. 3.

Figure 7. True target trajectories for 3g acceleration from 500 Monte Carlo runs.

Figure 8. True target trajectories for 4g acceleration from 500 Monte Carlo runs.

Figure 9. True target trajectories for 5g acceleration from 500 Monte Carlo runs.

Figure 10. Range measurement for 4g acceleration from 500 Monte Carlo runs.

Figure 11. True range for 4g acceleration from the first Monte Carlo run.
5.5.2. Azimuth Measurements
Azimuth measurements for the 4g acceleration scenario from 500 Monte Carlo runs are presented in Fig. 12. To explain the variation of azimuth with the measurement index, we present Fig. 13 with the beginning point of AB, midpoints of AB, BC, CD, DE, and EF, and the end point of EF. When the target is at A, the azimuth has a value of about 330 deg. As the target moves from A towards the midpoint of AB, the azimuth gradually increases to a value close to 360 degrees at $M_{1b}$, just before the midpoint of AB. At $M_{1b}$, just after the midpoint of AB, the azimuth has a value close to zero. As the target moves from the midpoint of AB to the midpoint $M_2$ of the arc BC, the azimuth gradually increases and reaches a local maximum at $M_2$. As the target moves from $M_2$ to the midpoint of CD, the azimuth gradually decreases to zero at a point $M_{3b}$, just before the midpoint of CD. Right after the midpoint of CD at $M_{3b}$, the azimuth is closer to 360 degrees. As the target moves to the midpoint $M_4$ of the arc DE, it reaches a local minimum. As the target moves from $M_4$ to the midpoint of EF, the azimuth reaches a value close to 360 degrees at a point $M_{5b}$, just before the midpoint of EF. Right after the midpoint of EF at $M_{5b}$, the azimuth is close to zero. After the midpoint of EF, the azimuth gradually increases as the target moves to F.

5.5.3. Radial Velocity Measurements
Fig. 14 presents radial velocity measurements for the 4g acceleration scenario from 500 Monte Carlo runs. For clarity of interpretation, we present radial velocity measurements for the 4g acceleration scenario from the first Monte Carlo run in Fig. 15. At point A, the angle between the target velocity and RLOS is greater than 90 degrees. Therefore, the target velocity has a negative component along the RLOS and the radial velocity at A is negative. As the target moves from A to the midpoint of AB, the angle between the target velocity and RLOS decreases and the radial velocity becomes more positive. From Fig. 3, the RLOS is tangent to the circular arcs BC and DE at G and H, respectively. Therefore, the target velocity and RLOS are parallel at these points. The radial velocity has local maxima at G and H. In Fig. 16, we have plotted the angle $\alpha$ between the velocity and RLOS from the first Monte Carlo run. We observe from Fig. 16 that at G, the angle $\alpha$ between the velocity and RLOS is nearly zero degrees. As the target moves from G to C the radial velocity decreases. The variation of radial velocity is similarly explained as the target moves from C to D, H, E, and F.
6. CONCLUSIONS

In this paper, we described details of the numerical simulation of a highly maneuvering target in 2D using the Bayesian framework. In our scenarios, the target can have accelerations of 3g, 4g, or 5g. The target has a sequence of nearly constant velocity (NCV) and nearly constant turn (NCT) motions. We used a fixed moving target indicator (MTI) radar to generate range, azimuth, and radial velocity measurements. In our simulation, 500 Monte Carlo runs were used to generate true trajectories and MTI sensor measurements. Our future work will focus on dynamic state estimation of a highly maneuvering target and performance evaluation of filtering algorithms for the problem.

7 REFERENCES

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CONTRIBUTORS

Radhika MN received the BE and M. Tech. degrees in electronics and communication engineering from Visvesvaraya Technological University (VTU), Belagavi, Karnataka, India in 2008 and 2011, respectively. Her research interests are estimation, linear and nonlinear filtering, maneuvering target tracking, guidance, multisensor multitarget tracking, and data fusion. She is currently pursuing the Ph.D. degree in University of Mysore. In the current study, she developed algorithms and Matlab code, analyzed numerical results, and prepared the manuscript.

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