

Harmonic Reduction In Multilevel Inverter Based On GA Optimization

Kishor bommassani, P. Ram Prasad

Abstract: This paper proposes a generalized formulation for Harmonic reduction-Pulse Width Modulation (HR-PWM) control suitable for high-voltage high-power cascaded multilevel voltage source converters (VSC) used in constant frequency utility applications. This utilizes the merits of the genetic algorithm (GA) in finding the optimal solution to the nonlinear equation system with fast and guaranteed convergence. This deals with different operation points for both five and seven level converters. The solution to the harmonic minimization problem using genetic algorithm optimization is determined

Keywords: Cascaded multilevel inverter, Hybrid Genetic Algorithm, Pulse width modulation, Selective Harmonic Elimination.

1 INTRODUCTION

Multilevel converters have drawn tremendous interest in recent years and have been studied for several high-voltage and high-power applications. Switching losses in these high-power high-voltage converters represent an issue and any switching transitions that can be eliminated without compromising the harmonic content of the final waveform is considered advantageous. The term multilevel starts with the introduction of the three-level converter. By increasing the number of levels in a given topology, the output voltages have more steps generation a staircase waveform, which approaches closely the desired sinusoidal waveform and also offers reduced harmonic distortion. One promising technology to interface battery packs in electric and hybrid electric vehicles are multilevel converters because of the possibility of high VA rating and low harmonic distortion without the use of a transformer. Harmonic Reduction-pulse-width modulation (HR-PWM) has been mainly developed for two- and three- level converters in order to achieve lower total harmonic distortion (THD) in the voltage output waveform. The main challenge associated with HR-PWM techniques is to obtain the analytical solution of the system for nonlinear transcendental equations that contain trigonometric terms which in turn provide multiple sets of solutions. Genetic algorithm has been recently introduced to optimize the sequence of the carrier waveform of the PWM as to minimize the THD and the distortion factor (DF) of output line voltage. An optimization technique assisted with a hybrid genetic algorithm was successfully applied to find the switching transitions (i.e., switching angles) of the HR-PWM ac/ac converter. More recently, a general genetic algorithm using Matlab GA optimization Toolbox was applied to solve the same problem of HR-PWM.

However, the solutions to the equal dc sources and with the fundamental frequency switching method which has lower degrees of freedom for specifying the cost function compared with the proposed PWM method for the same physical structure. Furthermore, hybrid genetic algorithm is applied to stepped multilevel converter with non equal dc sources in. As the primary limitation (disadvantage) of the stepped modulation techniques lies in its very narrow modulation index range, several works have been attempting to overcome this shortcoming. Specifically, proposed a modulation technique that widens the modulation index by swapping the polarity of some levels so that a low modulation index can be obtained and maintaining the fundamental switching technique. A new active harmonic elimination technique was recently introduced to the line frequency method aiming to eliminate higher order of harmonics by simply generating the opposite of the harmonics to cancel them. However, the disadvantage in that is that it uses a high switching frequency to eliminate higher order harmonics. Other approaches have also been reported, including one where the harmonic elimination is combined with a programmed method, and another where multilevel HR-PWM defined by the well-known multi carrier phase-shifted PWM (MPS-PWM) was proposed in, where the modulation index defines the distribution of the switching angles, and then the problem of HR-PWM is applied to a particular operating point aiming to obtain the optimum position of these switching transitions that offer elimination to a selected order of harmonics. By effectively solving the harmonic elimination problem with large number of switching angles, the HR-PWM method can generate high-quality voltage waveform as well as less switching frequency as compared to other modulation techniques. Fig.(1) Shows the structure of a single-phase multi-level cascaded inverter that consists of series connection of H- bridge inverter units. Each unit has its own separated dc source (SDCS), which may be obtained from an ultra-capacitor, battery, fuel cell, solar cell, etc. In order to generate the multilevel voltage waveform, the ac terminal voltages of different H-bridge inverters are connected in series and the overall output voltage van is given by the sum of H-bridge voltages. i.e., $v_{an} = v_1 + v_2 + v_3 + v_4 + v_5$.

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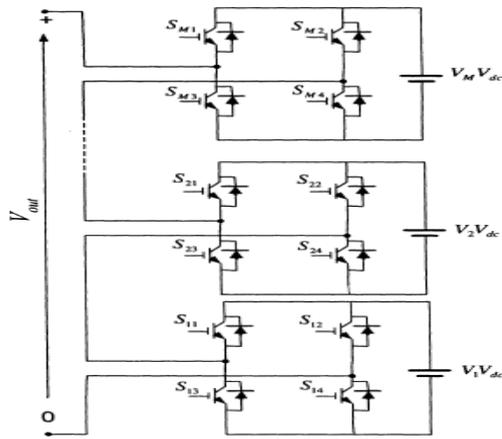


Fig1: Cascaded H-Bridge Multilevel Inverters

Each full bridge inverter can generate three different dc voltage levels of + Vdc, 0, and - Vdc in its ac terminal, which depends on the state of four power switches: Q1, Q2, Q3 and Q4. The number of levels of output phase voltage *m* in a cascade multilevel inverter is $m = 2s + 1$, where *s* is the number of SDCs.

II. ESTIMATION OF SWITCHING ANGLES

As per the Fourier theorem the periodic output voltage *V* (ωt) can be described by a constant term plus an infinite series of sine and cosine terms of frequency *n* ω , where *n* is an integer. Therefore *V* (ωt) in general, can be expressed as

$$f(\omega t) = \frac{a_0}{2} + \sum_{n=1}^{\infty} (a_n \cos n \omega t + b_n \sin n \omega t), \tag{1}$$

Because of the output voltage of the multilevel inverter is quarter wave symmetry, the Fourier series constants a_0 and a_n can become zero and only b_n is to be calculated. The value of b_n is found using the equations (2)

$$b_n = \frac{1}{\pi} \int_0^{2\pi} V_0(\omega t) \sin n \omega t \, d(\omega t), \tag{2}$$

Fourier series of the quarter-wave symmetric H-bridge multilevel inverter output waveform is written as given in equation (6) in which θ_s are the optimized switching angles, which must satisfy the following condition

$$\theta_1 < \theta_2 < \theta_3 \dots \dots \theta_s < \frac{\pi}{2} \tag{3}$$

The method to solve the optimized harmonic switching angles will be explained in this section. From equation

1. The amplitude of dc component equals zero.
2. The amplitude of all odd harmonic components including fundamental one, are given by

$$h(n) = \frac{4V_{dc}}{\pi} \sum_{k=1}^s \cos n \theta_k \tag{4}$$

3. The amplitude of all even harmonics equal zero. Thus, only the odd harmonics in the quarter-wave symmetric multilevel waveform need to be eliminated. The switching

angles of the waveform will be adjusted to get the lowest THD in the output voltage

$$h(n) = \frac{4V_{dc}}{n\pi} [\cos \theta_1 + \cos \theta_2 + \cos \theta_3 + \dots]$$

If needed to control the peak value of the output voltage to be *V*₁ and eliminate the fifth and seventh order harmonics, the modulation index is given by

$M = \frac{nV_1}{4V_{dc}}$ the resulting harmonic equations are

$$\frac{4V_{dc}}{\pi} [\cos \theta_1 + \cos \theta_2 + \cos \theta_3 + \cos \theta_4 \dots] = V_1 \tag{5}$$

$$\cos 5\theta_1 + \cos 5\theta_2 + \cos 5\theta_3 + \cos 5\theta_4 \dots = 0 \tag{6}$$

$$\cos 7\theta_1 + \cos 7\theta_2 + \cos 7\theta_3 + \cos 7\theta_4 \dots = 0 \tag{7}$$

Equation (5) is rewritten as

$$\cos \theta_1 + \cos \theta_2 + \cos \theta_3 + \cos \theta_4 \dots = M \tag{8}$$

Each H-bridge inverter unit has a conduction angle which is calculated to minimize the harmonic components the conduction angles are the factors determining the amplitude of the harmonic components. This paper deals with a H-bridge cascaded inverter because its multi-level output voltage can be almost sinusoidal. In that case the conventional method can eliminate the dominant harmonics except for the fundamental wave. In multi level inverter 'n' dc sources are needed so that the dc voltage levels are chosen so as not to generate the dominant harmonics while achieving the desired fundamental voltage. This is a system of three simultaneous equations with four unknowns $\theta_1, \theta_2, \theta_3, \theta_4 \dots$. These values are found by solving the simultaneous equations (5-7).

III. GA TOOLBOX

Genetic Algorithm (GA) is a method used for solving both constrained and unconstrained optimization problems based on natural selection, the process that drives biological evolution. GA repeatedly modifies a population of individual solutions. At each step, GA selects individuals at random from the current population to be parents and uses them to produce the children for the next generation. Over successive generations, the population "evolves" towards an optimal solution. GA uses three main rules at each step to create the next generation from the current population:

Selection rules select the individuals, called *parents* that contribute to the population at the next generation.

Crossover rules combine two parents to form children for the next generation

Mutation rules apply random changes to individual parents to form children.

Calling the function 'ga' at the Command Line To use GA at the command line, call the GA function *ga* with the syntax

$[x \text{ fval}] = \text{ga} (@\text{fitnessfun}, \text{nvars}, \text{options})$

Where

@fitnessfun is a handle to the fitness function.

nvars is the number of independent variables for the fitness function.

Options is a structure containing options for the genetic algorithm. If you do not pass in this argument, GA uses its default options. The results are given by

x — Point at which the final value is attained

fval — Final value of the fitness function Using the function GA is convenient if you want to Return results directly to the MATLAB workspace Run the genetic algorithm multiple times with different options, by calling ga from an M-file.

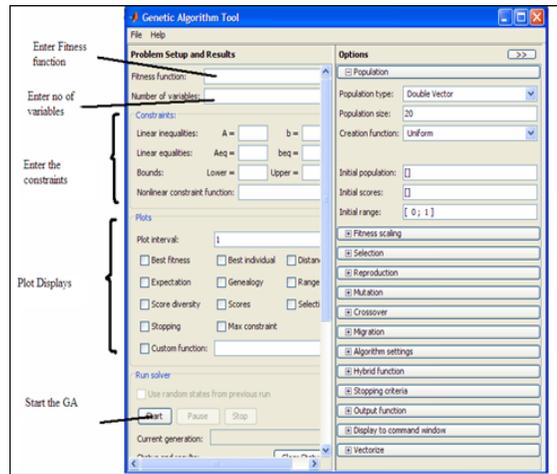


Fig.3: GA toolbox

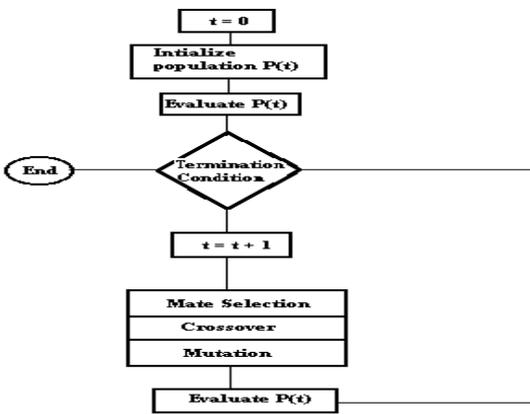


Fig2: flow chart of GA

Using GA Tool The Genetic Algorithm tool is a graphical user interface that enables you to use the genetic algorithm without working at the command line. To open it, enter *gatool*. at the MATLAB command prompt. The tool opens as shown in the Fig.2. To use the GA tool, the following information is entered,

Fitness function — The objective function is to minimize. Enter the fitness function in the form *@fitnessfun*, where *fitnessfun* is an M-file that computes the fitness function.

Number of variables — The length of the input vector to the fitness function. Enter constraints or a nonlinear constraint function for the problem in the **Constraints** pane. If the problem is unconstrained, leave these fields blank. To run the GA, click the Start button. The tool displays the results of the optimization in the Status and results pane. We can change the options for the genetic algorithm in the Options pane.

IV. MULTI-LEVEL INVERTERS

Simulation circuit for Three phases 3-level inverter:

Simulation of 3-level and 5-level cascaded multilevel inverter is done using simulink from MATLAB. IGBTs are chosen as switching device for simulation, since it has more features than the other power semiconductor devices.

Three-Level converter: A typical three-phase inverter designed in half-bridge topology (Figure 3) allows for an output voltage waveform that can switch between two voltage levels only. The topology in Figure 1b, by contrast, allows for an output voltage waveform that switches through three voltage levels, which is why this topology is also known as three-level inverter topology. We will now analyse the principle behind a three-level inverter in order to ascertain the differences between it and a conventional 2-level inverter [1]. For a three-phase three level inverter a structure similar to that used with 12 electronic devices (IGBT) is needed (see Fig 3). Each phase will switch across three voltage levels (+V_{dc}/2, 0, -V_{dc}/2).

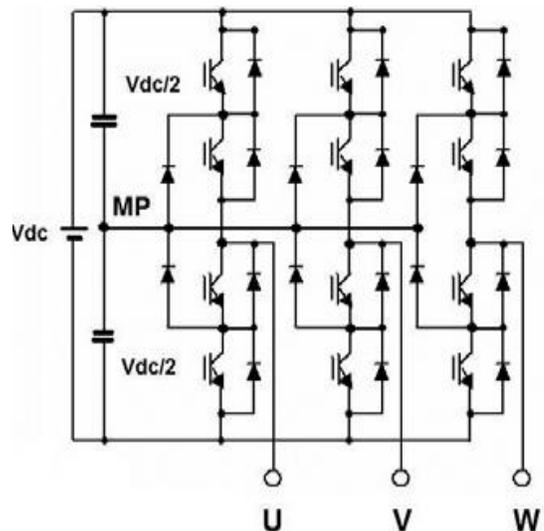


Fig.4: Three-Phase Three-Level Inverter Topology

In a structure such as this the maximum voltage across the IGBT is limited to half the maximum DC link voltage ($V_{dc}/2$). This is down to the fact that the IGBTs are connected to the neutral point (MP) by two fast diodes called neutral clamp diodes.

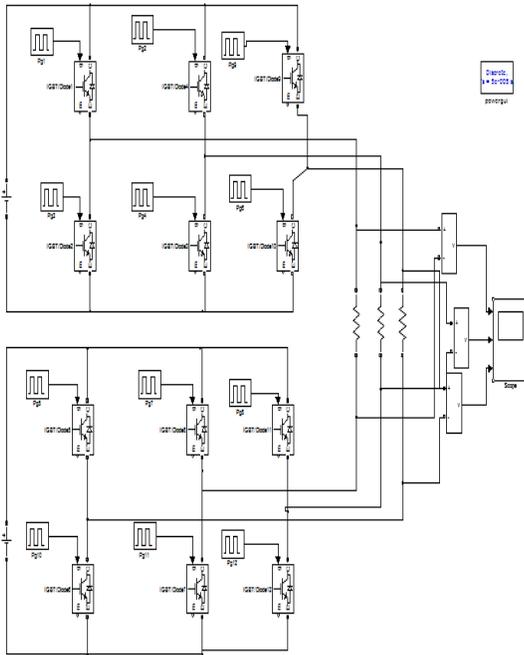


Fig5: Simulation circuit for three phase 3-level inverter

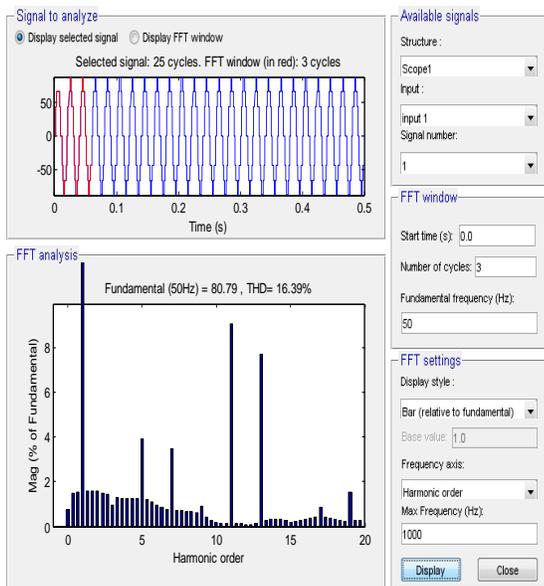


Fig6: Simulation Result For Three Phase 3-Level Inverter

GA results:

Objective function value: 1.19683556479E-4

The optimal firing angles are:

$\alpha_1=33.85$ and $\alpha_2=177.5$

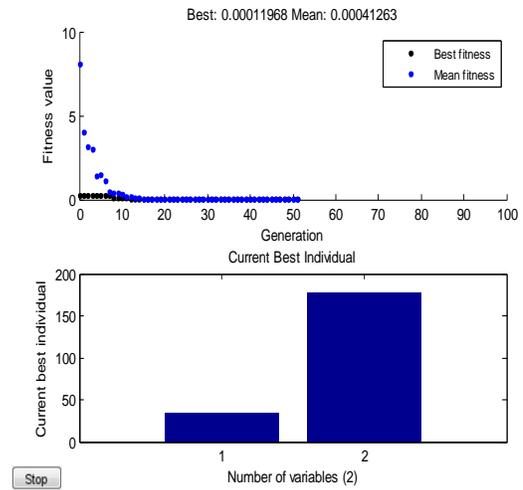


Fig.7: Best Fitness and Individual Plots

Five-Level Converter: In this case, the five-level output waveform is produced by connecting two H-bridge cells in series. First, it is assumed that each cell operates at a frequency of three times the fundamental; therefore, there are three switching angles per quarter-cycle at the output voltage of each cell (i.e., $N1 = N2 = 3$) producing an overall six angles per quarter-cycle of the five level waveform (i.e., $N = 6$). The optimization technique is applied to this case to find the optimal switching angles that eliminate five lower harmonics and controlling the fundamental. It is interesting to note that even though the solution does not exist for the whole region of modulation index, multiple sets of solution have been found as plotted. The investigation to define the optimal set that might have lower harmonic distortion is beyond the scope of this paper as its application dependant and will be addressed in future work.

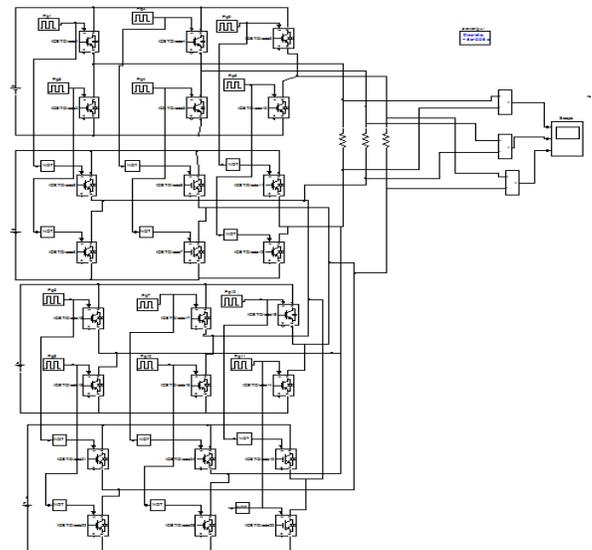


Fig8: Simulation circuit for three phase 5-level inverter

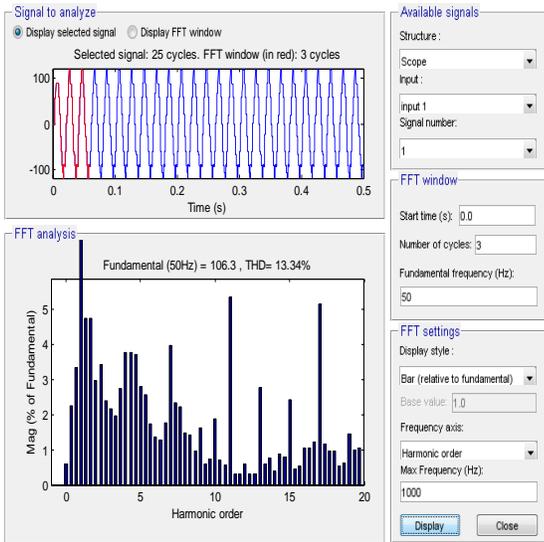


Fig9: Simulation result for Three phase 5-level inverter

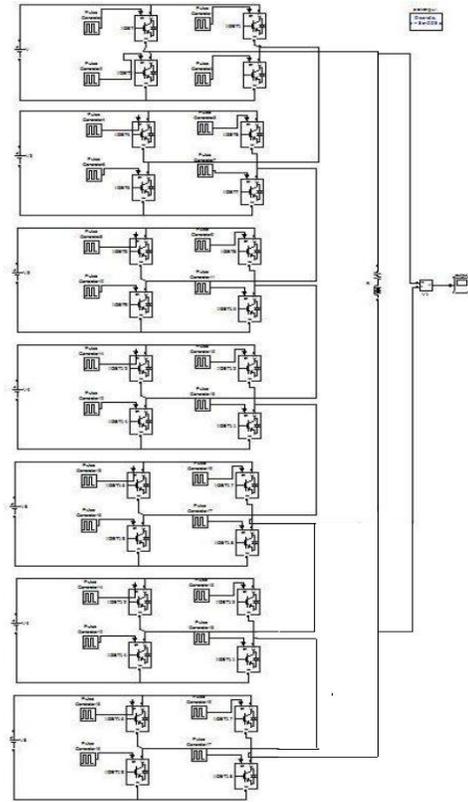


Fig11: Simulation circuit for Single phase 15-level inverter

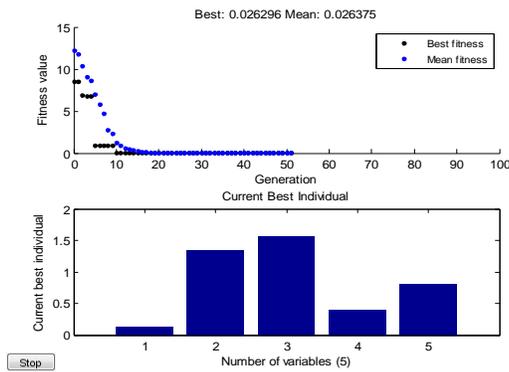


Fig.10: Best Fitness And Individual Plots

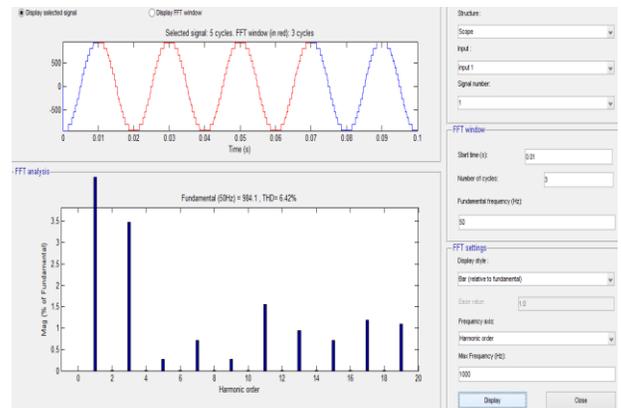


Fig .12 : Simulation result for Single phase 15-level inverter

GA results:

Objective function value: 0.026125005156022996
 The optimal firing angles are,

$$\alpha_1=65.96^0, \alpha_2=205.93^0, \alpha_3=294.92^0 \text{ and } \alpha_4=294.92^0$$

Simulation results for Single Phase 15-Level Inverter:

Simulation circuit for Single phase 15-level inverter is shown in fig. 11, which consist of 7casadded bridges. Simulation result for Single phase 15-level inverter is shown in fig. 12, best fitness and individual plots is shown in fig. 13.

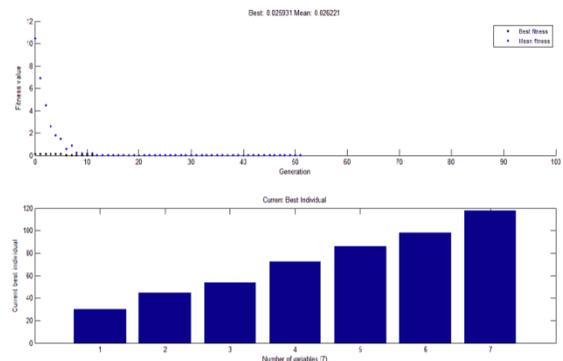


Fig.13: best fitness and individual plots

GA Results:

Objective function value: 0.026187093375983773

The optimal firing angles are,

$$\alpha_1=25.96^\circ, \alpha_2=45.453^\circ, \alpha_3=55.243^\circ, \alpha_4=74.854^\circ, \\ \alpha_5 = 85.543^\circ, \alpha_6 = 97.622^\circ \text{ and } \alpha_7 = 117.847^\circ$$

Comparison table for simulation results: THD values of 3,5 and 15 level inverter using PWM technique and Genetic Algorithm are given in Table1.

Table1: Comparison of simulation results

No. of levels	Phase	THD% using PWM technique	THD% using Genetic Algorithm
3-level	Three	35.01%	16.39%
5-level	Three	25.80%	13.34%
15-level	single	11.25%	6.42%

V. CONCLUSION

A generalized formula of Harmonic Reduction-Pulse width Modulation (HR-PWM) suitable for high-power high-voltage cascaded multilevel converters with equal dc voltage sources was proposed and demonstrated in this project. Using this GA optimal firing angles have been determined for various multi-level cascaded inverter topologies. These optimal firing angles are used for triggering the power devices (IGBT/diode). With this switching angles approximate sinusoidal output voltage and current waveforms with minimum amount of Total Harmonic Distortion (THD) have been achieved. The percentage of THD obtained in the output of multilevel inverter topologies using PWM technique is compared with that obtained in the output of multilevel cascaded inverters in which advanced Genetic Algorithm optimization technique is used. It is observed that nearly 70-80% THD in the output has been reduced by using Genetic Algorithm optimization technique as compared to that obtained from inverter topologies using PWM technique.

VI. REFERENCES

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