Implementation of Mathematics Learning Model Based on Theory: Action, Process, Object, Scheme (APOS Model) On Improper Integral Subject

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Abstract—The APOS model is a Mathematics Learning Model Based on Theory: Action, Process, Objects, Schemes with syntax consisting of phases: Orientation, Practicum, Small Group Discussion, Class Discussion, Exercise and Evaluation. The APOS model has been implemented in the Integral Calculus course by Class A 3rd Semester Students in the Mathematics Education Study Program FKIP UNIB 2018/2019 in the amount of 38 student. The APOS model is equipped with Integral Worksheet based on the APOS model consisting of 14 worksheets. Concept about improper integral was in 14th worksheet. Based on the poll results, the 14th worksheet was the most difficult worksheet so they are not tested on the Examination. Examination was held on December 6, 2018. After the final assessment is carried out, information was obtained that those who get the A- or A score were 15 people (39.47%). The purpose of this research was to find out whether students who get A- or A scores in the Integral Calculus course were able to solve the improper integral test questions. The test was held on February 2, 2019, and was attended by 12 students. Previously students were not notified of a test. The instruments of this research was test sheets, Likert scale questionnaires, and open questionnaires. After the data was processed, information was obtained as follows: there were 41.67% of students who still remember very well and got score $\geq 80$, and there were 16.67% of students who could remember well and got score $> 70$. Based on the result, it concluded that students who study the lesson before going to college from various sources, then active in small group discussions and presentation in front of the class would took longer to remember the lesson than students who were waiting for a friend's explanation in front of the class. These results prove the truth of Edgar Dale's Cone of Experience. The establishment of mutual assistance between students proved the truth about Vygotsky's social constructivism.

Index Terms—Improper Integral, APOS Model, APOS Models' Syntax, Integral Calculus Worksheet.

1 BACKGROUND

Integral calculus was a compulsory subject in Mathematics Education Study Program Faculty of Teacher Training and Education of University of Bengkulu with 4 (3-1) credit semester. The goal to be achieved after a student learns Calculus well is to acquire basic knowledge and mathematical mindset, in the form of: (1) the critical, logical, and systematic thinking of scientific thinking; (2) the trained of reason and creativity after studying the various strategies and tactics in solving the calculus problem; (3) trained in designing simple mathematical models; (4) skilled in standard technical math supported by correct concepts, reasoning, formulas, and methods. [8] The test result shows that there are 3 students who well-master about the improper integrals. Although after 2 months of semester off, and they do the test without learning first, AB, ET and RD still remember the improper integrals matter. So the goal of learning calculus well has been achieved. Nevertheless, two other students still lack the mastery of these lessons.[1] (Martono, 1999).

In the 2017/2018 Academic Year calculus integral learning was carried out by applying the Mathematical Learning Model Based on Theories of Action, Processes, Objects and Schemes (APOS Model). The APOS model was a refinement of the Calculus Learning Model Based on APOS Theory (MPK-APOS) [2] (Hanifah, 2016). MPK-APOS was equipped with Worksheet Based on APOS MODEL with Maple 11 Assisted which consists of 14 Worksheets that were valid, practical, and effective [3] (Hanifah 2015). The title of each worksheets were as follows: 1st worksheet was indefinite integral as antiderivate; 2nd worksheet was Extensive Introduction; 3rd worksheet was definite integral; 4th worksheet was Basic Calculus Theorem; 5th worksheet was Area-wide; 6th worksheet was Swivel Volume (1); 7th worksheet was Swivel Volume 2; 8th worksheet was Transcendent Function; 9th worksheet was Substitution Integration; 10th worksheet was Some Integral Trigonometry; 11th worksheet was Substitution Rationalizes; 12th worksheet was Partial Integral; 13th worksheet was Integral Rational Function; 14th worksheet was Improper Integral. Each worksheet was distributed to each group after students were in class and calculus integral learning was ready to learn.

Especially for 14th worksheet about improper integral, because on the Integral Calculus syllabus in the S1 Mathematics Education Study Program Faculty of Teacher Training and Education University of Bengkulu did not contain improper integral lesson, so 14th worksheet has not been implemented in the classroom. In order for 14th worksheet to be utilized, the authors asked the 5 best students during the class to do homework in groups about 14th
Improper Integral in TheFinite Interval
For the improper integral in the finite interval, we have 3 definitions.
For every $x > 0$ with $0 < x < b - a$, the function $f$ integrated in $[a + x, b]$, 
$$
\lim_{x \to a} f(x) = \pm \infty, \quad \text{and provided } \lim_{x \to a} \int_{a+\varepsilon}^{b} f(x) \, dx = \lim_{x \to a+} \int_{a+\varepsilon}^{b} f(x) \, dx = L.
$$
In this situation, the improper integrals in interval $[a, b]$ defined as $\int_{a}^{b} f(x) \, dx = \lim_{x \to a+} \int_{a+\varepsilon}^{b} f(x) \, dx = \lim_{x \to a-} \int_{a-\varepsilon}^{b} f(x) \, dx = L.$
It says the improper integral $\int_{a}^{b} f(x) \, dx$ converges to $L.$ Then if $\int_{a}^{b} f(x) \, dx = \lim_{x \to a+} \int_{a+\varepsilon}^{b} f(x) \, dx = \lim_{x \to a-} \int_{a-\varepsilon}^{b} f(x) \, dx = \pm \infty$ doesn't exist, the improper integral $\int_{a}^{b} f(x) \, dx$ said divergent.
For every $x > 0$ with $0 < x < b - a$ the function $f$ integrated in $[a, b - x]$, $\lim_{x \to a} f(x) = \pm \infty$, and if $\lim_{x \to a} \int_{a}^{b-x} f(x) \, dx = \lim_{x \to a} \int_{a}^{b} f(x) \, dx = L$ exist then so the improper integrals in interval $[a, b]$ defined as $\int_{a}^{b} f(x) \, dx = \lim_{x \to a+} \int_{a+\varepsilon}^{b-x} f(x) \, dx = \lim_{x \to a} \int_{a}^{b-x} f(x) \, dx = L.$
It says the improper integral $\int_{a}^{b} f(x) \, dx$ converges to $L.$ Then if $\lim_{x \to a} \int_{a}^{b-x} f(x) \, dx = \lim_{x \to a} \int_{a}^{b} f(x) \, dx = \pm \infty$ doesn't exist, the improper integral $\int_{a}^{b} f(x) \, dx$ said divergent.

Improper Integral in TheInfinite Interval
For the improper integral in the infinite interval, we have 3 definitions.

1) Let the function $f$ integrated for every $[a, b]$ and let $\lim_{b \to +}\int_{a}^{b} f(x) \, dx = L.$ the improper the improper integrals in interval $[a, \infty]$ defined as $\int_{a}^{b} f(x) \, dx = \lim_{b \to +} \int_{a}^{b} f(x) \, dx = L.$
It says the improper integral $\int_{a}^{b} f(x) \, dx$ convergent to $L$ then if $\lim_{b \to +} \int_{a}^{b} f(x) \, dx = \pm \infty$ or does not exist, the improper integral $\int_{a}^{b} f(x) \, dx$ said to be divergent.

2) Let the function $f$ integrated for every $[a, b]$ and let $\lim_{a \to -}\int_{a}^{b} f(x) \, dx = L.$ the improper the improper integrals in interval $[-\infty, b]$ defined as $\int_{a}^{b} f(x) \, dx = \lim_{a \to -} \int_{a}^{b} f(x) \, dx = L.$
It says the improper integral $\int_{a}^{b} f(x) \, dx$ convergent to $L.$ Then if $\lim_{a \to -} \int_{a}^{b} f(x) \, dx = \pm \infty$ or does not exist, improper integral $\int_{a}^{b} f(x) \, dx$ said to be divergent.

3) Let the function $f$ integrated for every finite intervals, with the improper integral $\int_{a}^{b} f(x) \, dx$ to be convergence to $L$ and $\int_{a}^{b} f(x) \, dx$ convergence to $M$. In this matter, the improper integral of function $f$ in $(-\infty, \infty)$ defined as $\int_{-\infty}^{\infty} f(x) \, dx = \int_{-\infty}^{a} f(x) \, dx + \int_{a}^{\infty} f(x) \, dx = L + M.$
It says the improper integral $\int_{-\infty}^{\infty} f(x) \, dx$ convergence to $L + M.$ if one of that integral's
divergence, so \( \int_{a}^{\infty} f(x) \, dx \) said to be divergence.

From the explanation above, it could be seen that the concept of improper integral was concept with a very high level of difficulty. Students must know where the function was defined, where the discontinuous function, how to calculate the limit, must be proficient using Integration Technique. For that we needed a learning model that could help students understand the concept properly.

In Indonesian Education system, teacher students sure need to practice learning that support the curriculum 2013 (K13) context in their lecture. In curriculum 2013, learning process must be focus on how students can develop their knowledge, skills, and good attitudes. In line with this orientation, learning in 2013 curriculum should be done through active and creative learning so that students can develop critical thinking skills and communication skills and develop creativity as well. There are at least five points that teachers must develop in teaching in order to get the realization of this learning. Those five points are: to observe with the approach of science, developing the ability to ask or intellectual curiosity, the ability to think, experiment, and communication [9].

Based on the explaining, Calculus Integral’s class did in applying APOS Model. The syntax of APOS model consists of phases: Orientation, Practicum, Small Group Discussion, Classroom Discussion, Exercise and Evaluation. The time division for each phase depends on the weight of the course credits, for Integral Calculus with 4 (3-1) credits, the 15 'Orientation phase, Practicum 50', Small Group Discussion 50', Break 15', 50th Class Discussion 'Exercise / Evaluation 20'.

APOS was a learning theory devoted to learning mathematics at the college level, which integrated the usage of computers, learning in small groups, and paying attention to mental constructions carried out by students in understanding a mathematical concept. These mental constructions were: actions, processes (processes), objects (objects), and schemes (schema) which were abbreviated as APOS [10] [11] [12] (Dubinsky, 2001; Arnawa, 2006; Suryadi, 2010).

Broadly speaking the characteristics of the Mathematical Learning Model Based on APOS Theory (APOS Model) were: (1) knowledge constructed by students through the APOS mental construction; (2) using syntax with phases: Orientetion, Practicum, Small Group Discussion, Class Discussion, Exercise, and Evaluation; (3) use a computer; (4) students study in small groups. The following was an explanation of the APOS Model Syntax [2] [3] (Hanifah, 2015; Hanifah 2016).

1) Orientation Phase. Lecturer activities were to prepare students to take part in learning by using the APOS Model Worksheet, as well as to explain the objectives of the study that week.

2) Practicum Phase. In this phase students carried out activities to work on the Maple command on the Worksheet in the Practicum phase. Maple’s answer was copied back to the place provided by the worksheet. The purpose of the practicum phase was to introduce new concepts, information, or situations. Practical activities were carried out in groups, with the division of tasks typing orders or copying Maple / Geogebra answers to tables that have been provided. In addition to computer labs, practicum could take place in the classroom, with students carrying laptops. During the practicum phase, the lecturer acts as a guide that ran from one group to another.

3) Small Group Discussion Phase. After the tables on the worksheet for the practicum phase were filled, in the small group discussion phase, the worksheet contains questions related to the contents of Maple’s execution table. Students were asked to discuss the answers to these questions in small groups. Discussions in small groups will help students found and constructed and understand the intent of the contents of the table. Through small group discussions, students were expected to be able to understand the concept of learning that was being discussed. To strengthen students’ understanding of a subject, questions were provided that would be solved manually without the help of Maple. Students were asked to discuss answers to the questions provided. For a subject that was not able to be explained by using Maple, it was the duty of the lecturer to provide assistance (scaffolding) about the subject matter.

4) Class Discussion Phase. In this phase the lecturer choose a group of students to explain in front of the class the answers of questions that were in the class discussion phase, or explain the results of work in their small group about solving questions manually . Another group of students listened and was given the opportunity to ask questions, or express opinions. Lecturers act as mentors who were ready to provide scaffolding if needed during class discussions.

5) Training Phase. The purpose of the Training phase was to strengthen students' understanding of a subject, which was discussed in the previous phase. In the Exercise phase, the lecturer gives questions taken from the practice questions. The limited time in class, the questions in the exercise could be used as homework. In completing homework, students were asked to study Calculus books, so that time and info limitations when in class could be completed by students from studying Calculus books at home.

6) Evaluation Phase The evaluation phase was the phase of the lecturer collecting information that could be used for decision making, whether the lesson could be forwarded or given assistance for improvement, or for other decisions. The APOS model has been applied to the Integral Calculus course and was supported by 14 Worksheets. When applying 14th worksheet about Improper Integral, the learning process was somewhat different from other worksheets. Recognizing that improper integral lesson was very difficult, and the worksheet designed for the practicum phase was also less supportive to assist students in understanding the lesson, in other words the Maple command that was chosen if the results were executed tends to be final results, it was deemed necessary to give scaffolding in the Orientation phase. Scaffolding was given by reminding by using the question and answer method, about the limit and continuity of functions at a point by drawing a discontinuous graph at some point. This condition was associated with an improper integral. There were several students who were able to answer these questions well by answering them on the board and explaining them. There were even students who already know how to solve questions about improper integral. After the assistance was given, students were asked to work on 14th.
worksheet which began with practicum using a laptop, then continued with a small group discussion phase, class discussion phase, and training / evaluation phase.

When it came to the class discussion phase, the selected group copied the results of their work on the board and explained them. Before they explained, the researcher first checked the results of their work, and straightens out if something got wrong. This was done in order to save time, and students explained the correct results. From the observation during the lecture, this class discussion phase was the phase awaited by students.

The density of integral calculus lesson, and the difficulty of integral lesson was not reasonable, making the writer took the decision that the improper integral lesson was not tested in the examination. Curiosity whether there were students who were able to solve improper integral problem, at the beginning of the class after the semester break, a test was held for students who get A or A- scores for integral calculus courses at 2018/2019. The number of participants should be 15 people, 3 people were absent, so 12 people participated in the test. Just like last year, the test was given after students returned to campus after the semester break. The test was also not informed beforehand so that no one brought the Calculus book. The aim of the research was to determine the implementation of the APOS Model assisted by the Integral Calculus Textbook on the subject of improper integral by 3rd semester students of class A Mathematics Study Program Faculty of Teacher Training and Education University of Bengkulu Academic Year 2018/2019.

2 METHODS

This research was an experimental research. Data collected in the form of quantitative and qualitative data. The instruments used to collect data were test sheets, Likert scale questionnaires, and open questionnaires.

2.1 Subject

The subject of this research was third semester students in class A Mathematics Education Study Program FKIP UNIB 2018/2019 who participated in the Integral Calculus class, and obtained an A or A-. The number should be 15 students, but 3 students were absent, so 12 students were carrying out an improper integral test.

2.2 Data Analysis Technique

The research data were analyzed in descriptively quantitatively. For data in the form of questionnaires using a Likert scale, data analysis techniques obtained were as follows [13] (Riduan, 2009).

a. Give a score for each item with an answer: strongly agree (5), agree (4), doubt (3), disagree (2), and strongly disagree (1).

b. Add the total score of each respondent to all indicators.

c. Granting scoresby:

\[ \text{Score} = \frac{\text{Getting Score}}{\text{Maximum Score}} \times 100\% \]

3 RESULT AND DISCUSSION

3.1 Result

a) Activity in Small Groups

The active discussion in small groups influenced the mastery of the lesson. This figure 1 follows about the activeness of high group students during Integral calculus learning.

![Activity in Small Groups](image)

From Figure 1 it could be seen that from 1st worksheet to 7th worksheet students were actively involved in small group discussions. After mid examination, starting from 8th worksheet to 12th worksheet, students activity decreased. 8th worksheet about Transcendent function was a new lesson that has never been taught in high school. 9th worksheet - 13th worksheet contained lesson about Integration Technique. Lesson about Integration Technique was something that has never been taught in high school, and has a high level of difficulty. 14th worksheet concerning improper integral was also new and most complicated lesson. Scaffolding given in the Orientation phase could enable students to actively discuss in small groups. Some students had already learned it from various sources before the lecture takes place. Those who have learned this encourage a teammate to be active in small group discussions. They also explained in front of the class during the Class Discussion phase.

b) Phase of Students Began to Understand Improper Integral Lesson

The following of figure 2 described what phase of the APOS Model students began to understand Integral Improper Integral Lesson.
Based on Figure 3, it could be seen that, there were three students who were able to answer correctly improper integral question even though the distance between completing the 14th worksheet in the class with the implementation of the test distance was almost 2 months. The following was a form of student answers.

<table>
<thead>
<tr>
<th>Code</th>
<th>Score</th>
<th>Answers (question)</th>
<th>Mistaken of Student’s Answers</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>1</td>
<td>2</td>
</tr>
<tr>
<td>X5</td>
<td>80</td>
<td>T</td>
<td>F</td>
</tr>
<tr>
<td>X8</td>
<td>30</td>
<td>F</td>
<td>F</td>
</tr>
<tr>
<td>X9</td>
<td>73</td>
<td>F</td>
<td>T</td>
</tr>
<tr>
<td>X15</td>
<td>30</td>
<td>F</td>
<td>F</td>
</tr>
<tr>
<td>X17</td>
<td>37</td>
<td>F</td>
<td>F</td>
</tr>
<tr>
<td>X19</td>
<td>73</td>
<td>F</td>
<td>F</td>
</tr>
<tr>
<td>X20</td>
<td>100</td>
<td>T</td>
<td>T</td>
</tr>
<tr>
<td>X23</td>
<td>100</td>
<td>T</td>
<td>T</td>
</tr>
<tr>
<td>X26</td>
<td>30</td>
<td>F</td>
<td>F</td>
</tr>
<tr>
<td>X27</td>
<td>50</td>
<td>F</td>
<td>F</td>
</tr>
</tbody>
</table>
From the table above, it could be seen that there were 5 students (41.67%) who still remember very well the improper integral lesson, and there were 2 students (16.67%) who could remember well. Even though the test was not informed beforehand and students also did not bring calculus books during the test. It was also seen that there were more students who remembered well than those who did not remember them anymore, which were 41.67%.

To find out more about what made them remember or forget, an open questionnaire was given. Questionnaire was analystic using percentage of the answer from the student who got score more than 70 and student who got score less than 70. The following explaining was the results of an open questionnaire.

Question number 1 was “Are you having trouble answering the question above? What is the reason?”. Students who got score ≥ 70 answered that 100% they felt the questions were difficult, but then they tried hard to remember it again. Students who got score < 70 answered that 100% they were in trouble, it happened because during the holidays they did not open the calculus book so they forgot the lesson.

Question number 2 was “When did you understand how to solve a similar problem above? (Choose one of the phases: Orientation, Practicum, Small Group Discussion, Class Discussion, Exercise / Evaluation).” Students who got score ≥ 70 85.71% said they began to understand in small group discussions, 14.29% had begun to understand in small group discussions, but really understood in class discussions. There was mutual assistance and sharing knowledge between teammates. In class discussion there was additional knowledge gained from the presentation group so that they knew more about the right way and results in solving the problem. Students who got score < 70100% just understood in the Class Discussion phase. Explanation of friends in front of the class made the obscure lesson clear.

Question number 3 was “Have you ever explained to a small group friend how to solve a similar problem above? What is the reason?”. Student who got score ≥ 70 answered 100% ever. When they understood and other friends did not understand, they helped friends by explaining it to other friends. Student who got score < 70 answered 100% ever for easy questions. Because sharing assignments to explain in small groups.

Question number 4 was “Is there any influence on your reasons for question 6 on ability to remember how to solve the above questions?” 100% Student who got score ≥ 70 said that has an effect. 100% Student who got score < 70 answered has no effect, because improper integral was not easy.

“If you have explained to a friend, is there any influence on your activities in learning the integral calculus? Give reasons for your answer” was the question 5. 100% student who got score more that 70 said it has an effect. The more understanding the lesson would be able to solve other questions and be more confident. For student who got <70, 100% student said it has an effect. They just explained if they understand the lesson. When explaining they became more understanding and better understand what is learned, and want friends to answer other questions. It made their confidence increased.

The 6th question was “What preparation do you make so you can explain in small groups or in front of the class?” For student who got score more than 70, they were learning through videos and discussions with friends and lecturers. They understood the lesson first and answer questions repeatedly. Student who got score less than 70 said that they studied at home and practice.

The last question was “Is there any influence explaining in small groups or in front of the class of your ability to solve problems?”. Student who got more than 70 said 100% has an effect. The other said 100% has no effect.

### 3.2 Discussion

Judging from the level of difficulty of the Worksheet, students used the 14th worksheet which was improper integral calculus as the most difficult worksheet. Although in reality the improper calculus was the most difficult lesson, it turns out that there were some students who were able to understand it and were able to explain it well in front of the class. Some of these students had prepared themselves to progress later in the presentation phase by learning the improper integrals from the source book, asking the senior students who have learned improper integrals, learning from videos on youtube. The independent attitude arisen as a result of previous learning where students must be prepared to explain how to solve an improper integral in front of the class if the lecturer is appointed at the presentation phase. This reinforces the results of the study [14] Hanifah (2019) which concluded that the APOS Model has a syntax with phases: Orientation, Practicum, Small Group Discussion, Class Discussion, Exercise and Evaluation. The APOS model was supported by the APOS Model Based Worksheet. The impact of applying the APOS Model on Integral Calculus learning was the formation of critical, resilient, confident and independent characters. Independent was meant to be able to find information from source books or from lab results or from other sources to solve the problem of Integral Calculus being studied.

Based on the results of the tests contained in Table 1 above, it showed that the theory of learning cones as shown in figure 6 below was proven to be true.
Students who tried to understand the lesson by learning it from various sources and explaining it in front of the class, it turns out that they remember the lesson longer. They could solve improper integral questions correctly, even though it has been two months since they studied the lesson. The value they obtained from the results of tests on improper integrals was $\geq 70$. There were even 40% who scored 100. The group with a score of $\geq 70$ said that 85.71% had begun to understand since the small group discussion phase. They said that when they explained to other friends, they became more understanding and more confident. For groups that have a value of $<70$, they said they didn’t remember the lesson because during the holidays they no longer open the Calculus book. When they were in the class, they could handle the lesson after listening to the explanations from their friends both in small groups and in class discussions. Only really understood in the class discussion phase. This meant that they did not try to find it by reading a book or watching a video, but waiting for an explanation from the presentation group. Based on the research did by [4] Hanifah (2018), we conclude that mastery of the lesson was in category “very effective”. The responses from the questionnaire, showed that the worksheet based on the APOS Model was effective to help the development of independent, diligent, thorough, resilient, responsible, jointly active, helpful, critical and creative characters of students. So, the APOS Based Worksheets was effective to use in calculus class on the Improper Integral lesson. The worksheet effectiveness also seen from the formation of independent, diligent, thorough, resilient, responsible, active cooperate, help each other, critical and creative characters of calculus students. Vygotsky in [15] Dagar and Yadav (2016) opinion that, Vygotsky views the origin of knowledge construction as being the social intersection of people, interactions that involve sharing, comparing and debating among learners and mentors. Hrouga highly interactive process, the social milieu of learning is accorded center stage and learners both refigure their own meanings and help others find meaning. In this way knowledge is mutually built. His view is a direct reflection of Vygotsky’s sociocultural theory of learning, which accentuates the supportive guidance of mentors as they enable the apprentice learner to achieve successively more complex skill, understanding, and ultimately independent competence (Dagar and Yadav, 2016). Vygotsky asserted that knowledge can’t be isolated from social and cultural context. He argues that all higher mental functions are social in origin and are embedded in the context of sociocultural setting. In social constructivist model, the knowledge is constructed through interaction between teacher and student. He role of teacher in social constructivist approach shis from the sole dispenser of knowledge to motivator, guide and resource person. Constructivism emphasizes on learner centered, learner directed and collaborative style of teaching learning process in which learning is supported by teacher s gaining authentic tasks. As Vygotsky famously stated, “Every function in the child’s cultural development appears twice: first, on the social level, and later, on the individual level; first between people …, then inside the child” [17] [22] According to Vygotsky, students develop higher mental functions through mediated, social and collaborative activity. Thinking and reasoning emerge through practical activity in the social environment and in relation to the cultural, historical, and lesson reality of the activity. Vygotsky defines ZPD (Zone of Proximal Development) as “the distance between the actual developmental level as determined by independent problem solving and the level of potential development as determined through problem solving under adult guidance, or in collaboration with more capable peers”. So we need learning lessons that allow learners and teachers to shift within the zone of proximal development gaining relational understanding of the content studied in that particular topic [19] [24] in this research, we had used a worksheet and computer application and its works in our students learning.

4 CONCLUSION

APOS model with syntax which consists of: Orientation phase, Practicum phase, Small Group Discussion phase, Class Discussion phase, and Latiham / Evaluation phase, has been applied to third semester grade A students of Bachelor’s Degree Mathematics Education Study Program Faculty of Teacher Training and Education University of Bengkulu 2018/2019. After the data was processed, the information as follows: there were 41.67% of students who still remember very well and got score $\geq 80$, and there were 16.67% of students who could remember well and got score $> 70$. Based on the result, it concluded that students who study the lesson before going to college from various sources, then active in small group discussions and presentation in front of the class would took longer to remember the lesson than students who were waiting for a friend’s explanation in front of the class. These results proved the truth of Edgar Dale’s Cone of Experience. The establishment of mutual assistance between students proved the truth about Vygotsky’s social constructivism.

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